2023

## Chen-Jung Hsu Lectures





## Persi Diaconis

Stanford University

## The Mathematics of Shuffling Cards

(Wed.) Mar. 8, 15:30 - Adding Numbers and Shuffling Cards (Thu.) Mar. 9, 15:30 - Adding a List of Numbers (and Other Determinantal Point Processes) (Fri.) Mar. 10, 15:30 - Shuffling Cards and the Geometry of Hyperplane Arrangements

Venue: Room 202, 2F, Astronomy-Mathematics Building (NTU Campus) 天文數學館二樓 202 演講廳(台大校區)

often is there a carry and if there is just a carry explain, 'it's all related to shuffling cards.' is it more or less likely that there will be carry next?' It turns out that carries form a Markov Lecture 3 Consider a collection of affine hyperchain with 'an amazing transition matrix' This planes in d-dimensional Euclidean space. This same matrix comes up in analyzing the usual divides space in chambers (points not on any of method of riffle shuffling cards. I will explain the hyperplanes) and faces. There is a natural the connection and 'the seven shuffles theo- projection operation (Tits projection): given a rem' 'in English' for a general audience.

in tracking the carries when a single column of Markov chain on chambers. Believe it or not, digits is added(!) It turns out that the carries this encompasses a huge collection of natural process forms a determinantal point process. Markov chains--including riffle shuffling, but Such processes occur in describing the energy also the Tsetlin library of computer science, the spectrum of atoms, in random matrix theory, in Ehrenfests urn process of statistical physics and describing the zeros of Riemann's zeta function hundreds of others. There is a complete theory and in hundreds of other applied problems. of such chains (closed form expressions for all They admit a general theory. Going back to

Lecture 1 When numbers are added in the carries, it turns out that 'carries are cocycles' usual way, 'carries' accrue along the way. Car- and the whole story works for any finite group iar-Mahadahn) lead to abstractions of general ries make a mess and it is natural to ask 'how and subgroup (and more generally yet). As I will ideas of modern algebra (such as Hopf algebras

face and a chamber, there is a unique chamber, adjacent to the face and closest to the starting Lecture 2 There is interesting math to be found chamber. Picking faces randomly induces a the eigenvalues, sharp rates of convergence,

...). Generalization of this set up (due to Aguand Lie algebras). Again, I will try to explain things for a general mathematical audience.

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